

# Agreeing about climate change

MATHEMATICS COULD HELP NATIONS COMMUNICATE AND CONCUR ON REDUCING CARBON EMISSIONS, SAYS S ANANTHANARAYANAN

Countries across the world have seen great improvement in wellbeing and comforts over the last century, but at the cost of huge consumption of energy and the resulting harm to the environment. In international parleys to limit carbon emissions, there are conflicts of interest, with less developed nations asking to be allowed to catch up and developed nations also seeking not to be loaded with more reductions than others.

While it is correct that agreeing to reduce emissions would have economic and political consequences, not reaching an agreement would do nobody any good. The need is clearly to discover the levels of reduction where the interests of all players are best met, but the last several rounds of international conferences under the aegis of the United Nations have to not been able to get nations to agree to how much each one needs to do.

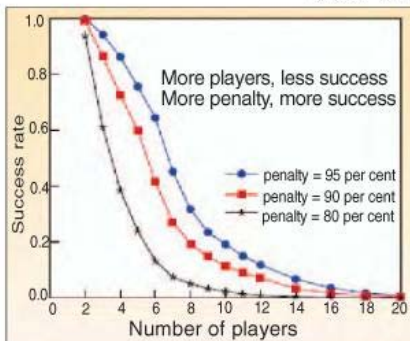
Rory Smead, Ronald L Sandler, Patrick Forber and John Basl of Northwestern and Tufts Universities in Massachusetts, in a paper in the journal *Nature Climate Change* examine the mathematical models of the interplay of nations and propose an alternative, iterative process for arriving at a stable international climate agreement.

Game theory is the mathematical bases for players in a game, where one player wins at the cost of the other (or others), to plan their strategy. The best strategy of each player would clearly depend on the best strategy of the other player, and a player should choose moves where he/she maximises gain, or minimises loss, despite the best moves by op-

ponents. If there is a single, best move, of both, which satisfies this condition, then they should clearly make this play all the time. But in most games, as in the marketplace, there is value in being unpredictable and the best strategy is a collection of moves, to be played in some proportions, but randomly. A pay-off table, where the result of each move by either player is shown, helps work out the best strategy for each player. And then there are bargaining games, in the simplest of which two players need to cooperate so that the result is better than sticking to one's place, which would result in both being the losers. A classic example of this kind is the so-called *Battle of the sexes*, where a husband and wife have a choice between a football game and the opera, the husband likes the game and the wife the opera. They would still like to go to the same place, and need to meet at the stadium or the theatre, but cannot communicate. If they go to different places, they both lose, and if they both land up at either, then one of them is a loser. And worse is if the husband goes to the theatre but the wife goes to the stadium, leaving both unsatisfied despite good intentions.

This game can be refined by assigning a value to the husband's pleasure at the football game and some pleasure at the opera (pleasing the wife is not a bad thing) or the wife's enjoyment of the opera and some interest in football, too. In such cases, it turns out that the best strategy is for the husband and wife to head for one or the other place according to some proportions.

The Massachusetts group notes in



Share of two out of eight	25%	40%	50%	66%
Frequency of success	0.1982	0.2173	0.2885	0.6143

In an eight-player negotiation, the success rate increases when just two are assigned increasing shares

		OPPONENT		
		A	B	C
PLAYER	A	3	2	1
	B	4	3	4
	C	5	2	2

The player wins at least 3 by playing "B". The opponent also loses the least by playing "B". Any other play by either can lead to a loss. The middle square, where "lowest" meets "highest, is known as the "saddle point".

the paper that for resolving the deadlock in climate negotiations, modelling has attempted to bring the various factors into classic games, like the *Prisoners' Dilemma*, or some other coordination games or games of conflict. The *Prisoners' Dilemma* is one where two criminals have been caught and the police is trying to get them to admit the crime. As neither obliges, they make them an offer — if either one confesses, but the other holds out, the one that confesses goes free but the other gets 20 years. If both confess, they get a light sentence

of one year. But if both hold out, they go free. Each prisoner's interest lies in confessing. If the other does not confess, the one that does goes free. Else he gets one year, but he is always safe from the 20-year sentence. The police, hence, usually solve the case, except when the prisoners have been indoctrinated or otherwise motivated to behave other than in the "rational" way.

The Massachusetts group has made a break from this pattern by using a version of the *Nash Bargaining*

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ations, the goal is a shared concern of reduction of total emissions and there is an all-round urgency in arriving at an agreement. In the model now developed, the payoff to each player was computed as proportionate to the player's demand, if the total demand was below the target, but with a penalty if the target was exceeded. Computer simulations of bargaining according to this model have revealed the effects of the numbers of players, the distribution of demand and also the level of penalty fixed for not keeping within the target, on the possibility of an agreement that satisfies requirements. The target was fixed at emission reduction by 50 per cent and success was when the players got within a per cent of the target in 100 rounds of negotiations.

A first result of the simulations was that the chance of agreement drastically reduces as the number of players increases. This points to a need to reduce the number of effective players in the game, in our case by creating "out of court" mergers. Thus, it would help if the number of nations was divided into groups that conducted their own negotiations and participated in the UN round as a single player.

The second factor was the penalty assigned to the total emissions being above target, which would amount to dissemination to all countries, the cost that each one pays if the world does not agree to stay within the target. A low penalty level reduced the chances of agreement, as disagreement did not lead to substantial reduction of payoff. The more the comprehension and perception of the cost of not agreeing, the greater the chances of successful negotiations. It was also seen that the initial starting point was crucial — if many players started out with high demands, negotiations usually broke down. There is, hence, the need for mechanisms to restrict initial demands, to help negotiation find a solution. Another factor that affects success was the heterogeneity of the players, or the mix of large players and small ones. This makes sense, as having more large players is effectively to have fewer players.

"Our model addresses the possibility that the problem in reaching an international climate agreement is not one concerning the existence of successful solutions but of realising them in negotiations," say the authors of the paper.

		OPPONENT	
		Heads	Tails
PLAYER	Heads	Win	Win
	Tails	Lose	Lose

In this game, the winning strategy is to actually toss a coin and play "heads" and "tails" at random

*Game*, in the simplest form of which two players make bids to claim parts of some limited resource, say money. If the total asked for is less than what is available, they can do better and the one that asked for less is likely to raise his/her demand a lot. If the demand is more than what there is, then there is a penalty, and there is an incentive to reduce the demand. While earlier analyses of the climate problem looked at preferred solutions that satisfy various conditions, they did not consider the dynamics of arriving at the solutions. The Massachusetts group looked carefully at how players may adapt to each others' behaviour and the process of deciding how to change bids while bargaining, in this case, for the least emission reduction by each to reach a given total reduction goal.

## Bargaining game

The extreme case of a bargaining game is where one player is inflexible and the other must either lose everything or agree for a small share. This sometimes happens in market situations where a larger player has more staying power. But in climate negoti-



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